

# Modelling historical changes in the water use efficiency of plants and ecosystems with different vegetation models

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<sup>2</sup>Centre for Ecology & Hydrology, Wallingford (UK)

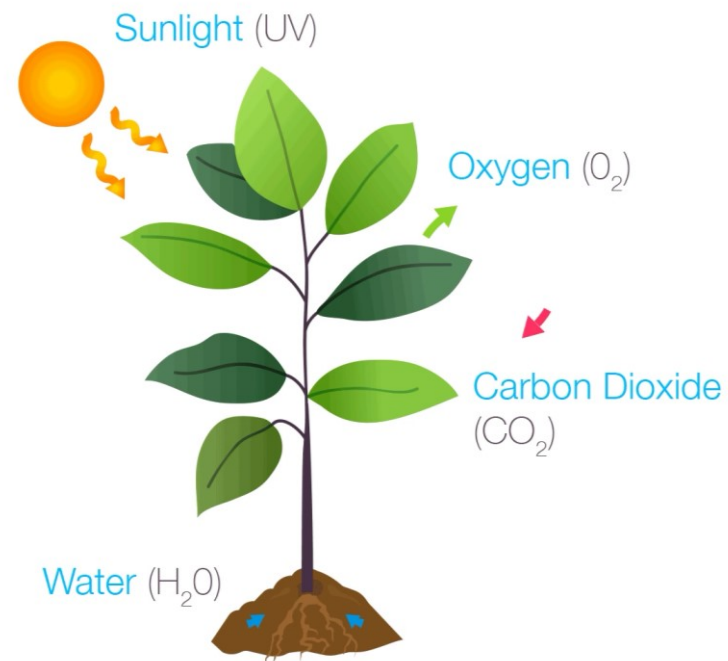
<sup>3</sup>Department of Physics, Imperial College London (UK)

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## Coupling the Carbon & Water Cycles

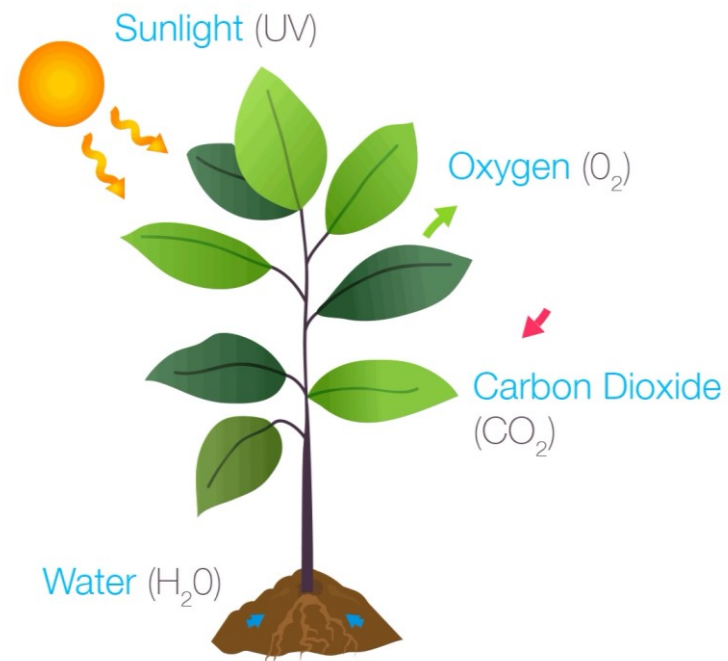
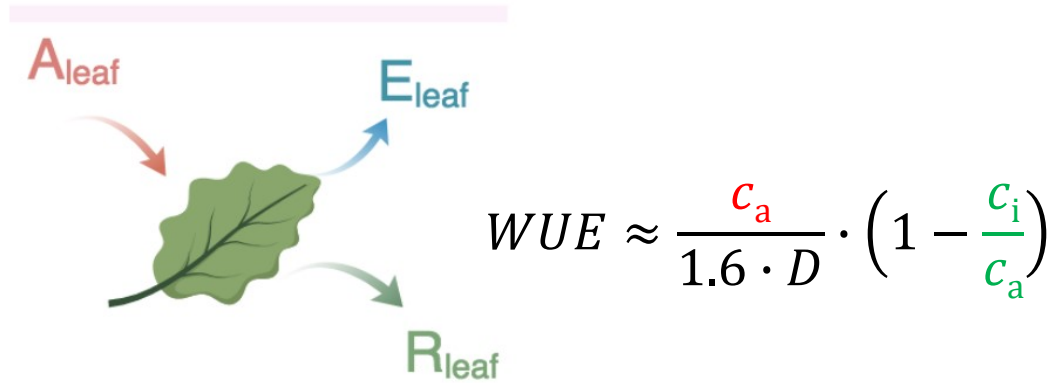
$$WUE = \frac{CO_2}{H_2O}$$



# Coupling the Carbon & Water Cycles

$$WUE = \frac{A}{E}$$

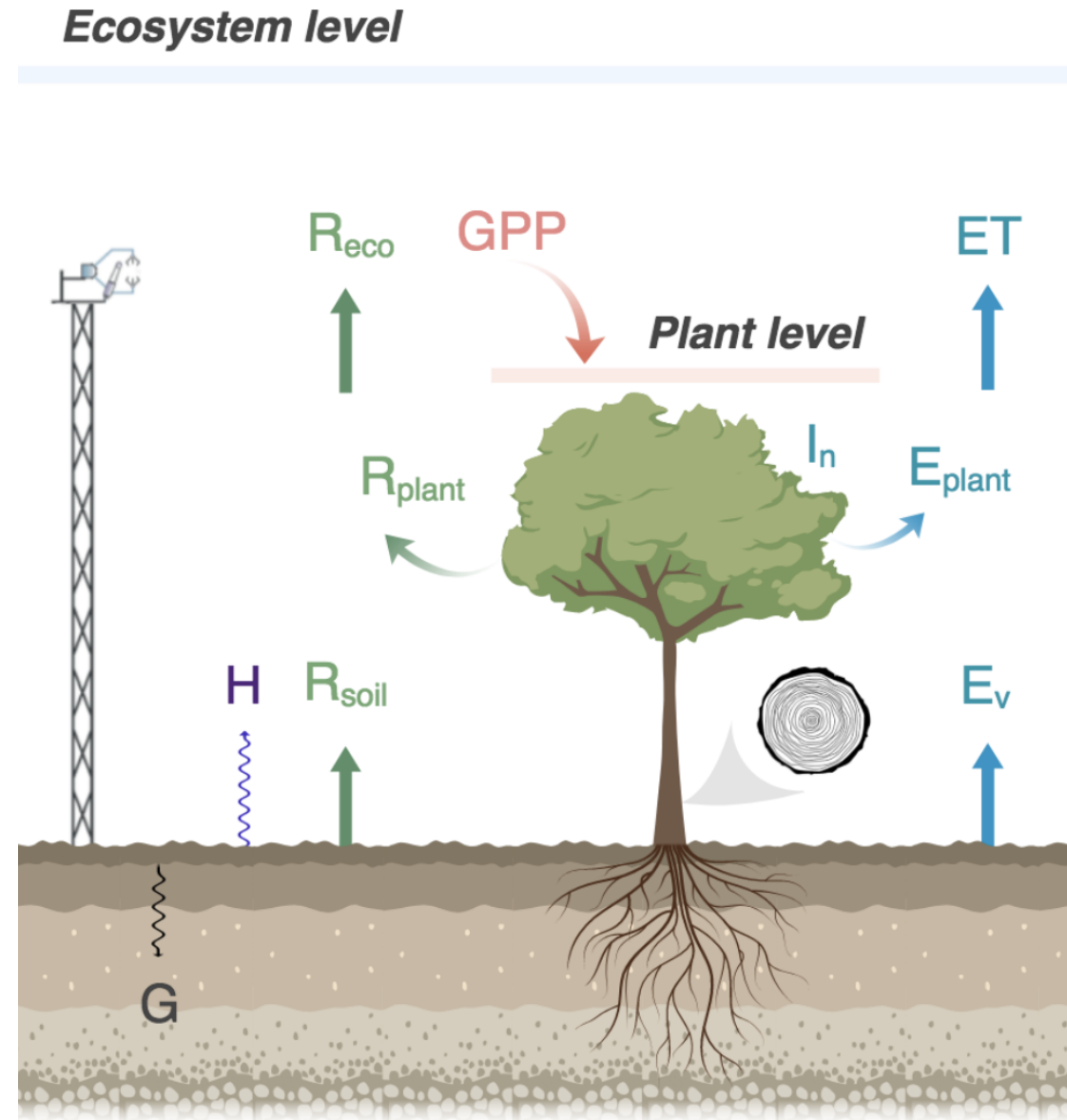
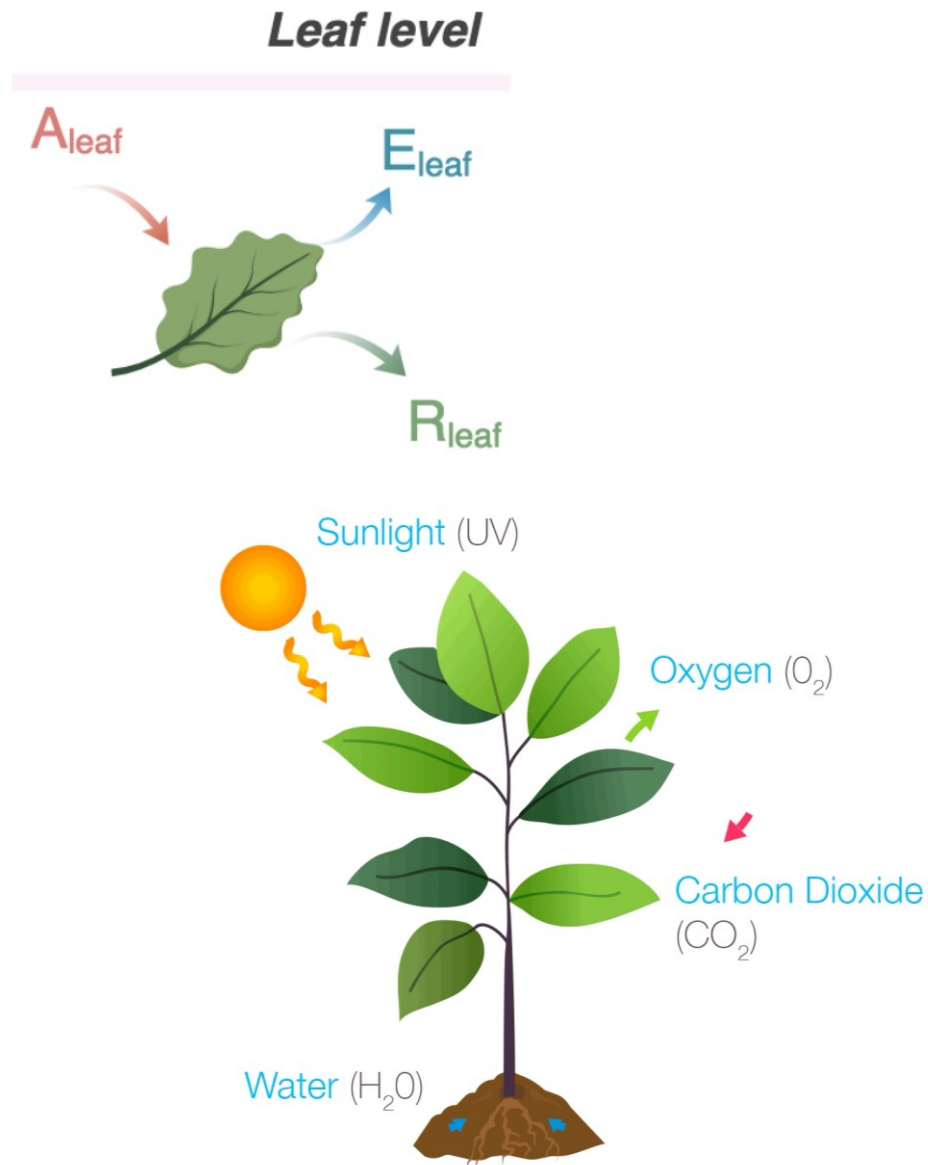
## Leaf level



A: photoassimilation rate; E: transpiration;  $c_a$ : atmospheric  $CO_2$  concentration;  $c_i$ : intercellular  $CO_2$  concentration;  $D$ : vapour pressure deficit

Coupling the Carbon & Water Cycles

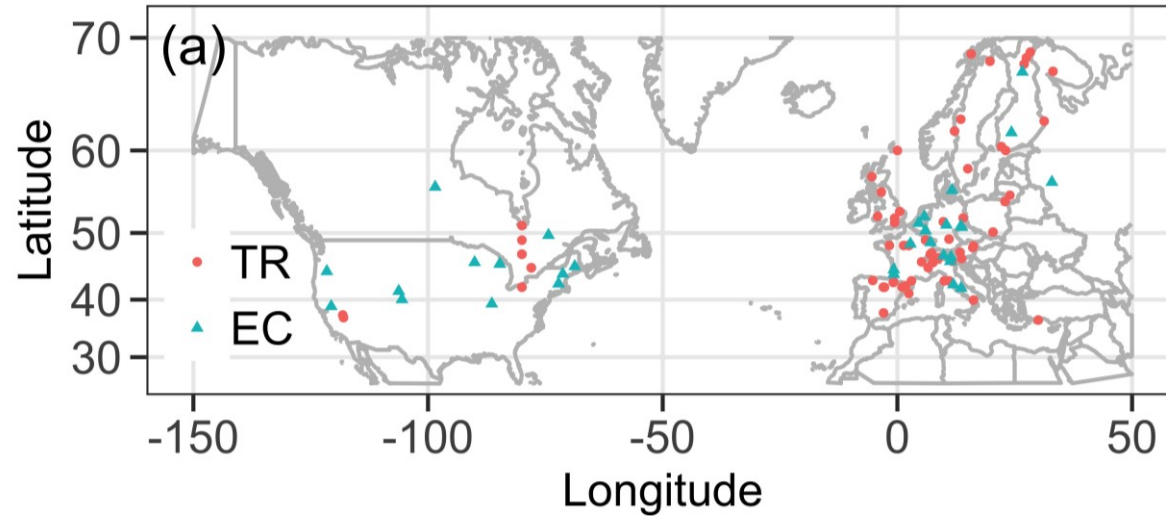
Ecosystem level

$$WUE = \frac{GPP}{ET}$$


GPP: gross primary production; ET: evapotranspiration

# Coupling the Carbon & Water Cycles

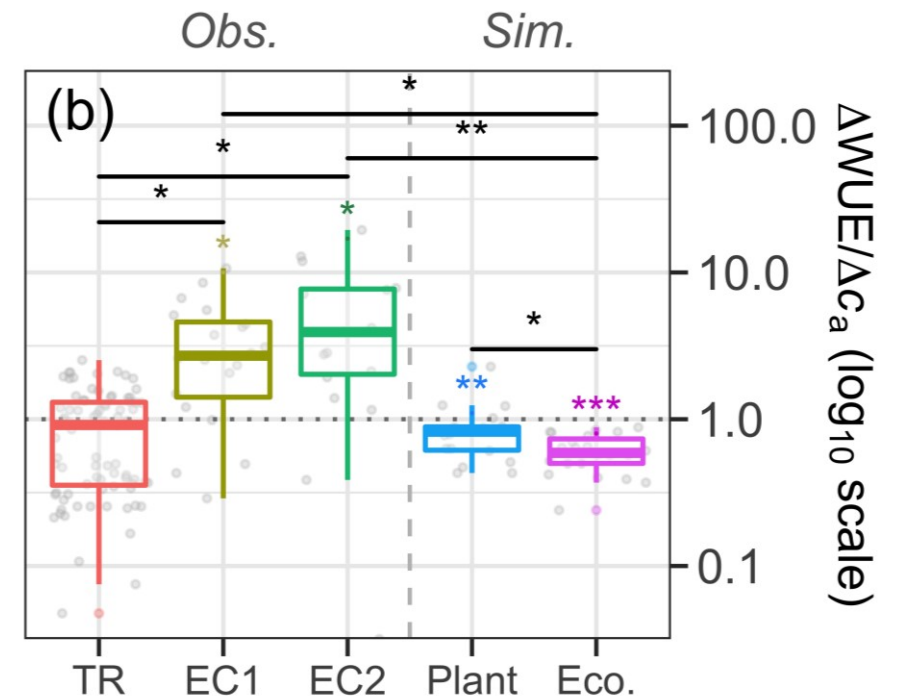
What are the relative contributions from environmental drivers?



EC: eddy-covariance flux data  
TR: carbon isotopes in tree rings

- Discrepancies in magnitude of changes in WUE between different types of observations
- Underprediction by vegetation models

Lavergne et al. (2019) *GCB*



# Coupling the Carbon & Water Cycles

Are the dependencies of WUE on CO<sub>2</sub> and *D* the same at leaf and ecosystem levels?

→ Contributions from CO<sub>2</sub> (*a*) and *D* (*b*) to WUE

$$\text{WUE}_T = \frac{c_a}{1.6 D} \left(1 - \frac{c_i}{c_a}\right)$$

$$\ln \{1 + f\text{WUE}\} = a \ln \{1 + fc_a\} + b \ln \{1 + fD\}$$

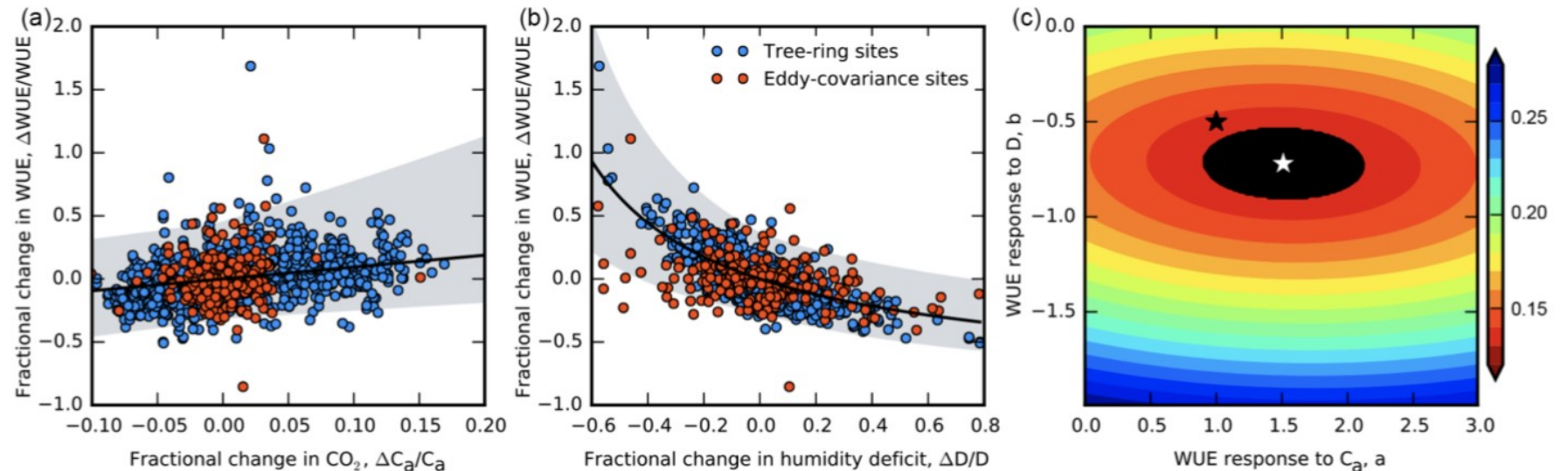
Fractional changes

$$fX = \frac{X - \bar{X}}{\bar{X}}$$

Values (mean ± sd) from 31 TR and 28 EC observational series over 1900-2010:

$$a = 1.51 \pm 0.57$$

$$b = -0.72 \pm 0.16$$



→ Testing the performance of different types of vegetation models to predict the environmental dependencies of WUE **at the leaf and ecosystem levels**

### How?

→ Estimation of contributions from  $\text{CO}_2$  and  $D$  on WUE from:

1. independent networks of **TR** (leaf-level) and **EC** (ecosystem-level) observations over their common period of records (1991-2014)
2. vegetation model outputs

→ Model-data comparisons



vn4.6

- fixed land cover map
- prescribed leaf area index (LAI) → seasonal variations derived from phenology model but no year-to-year variations
- **distinction among plant functional types (PFTs) : fixed parameters defining behaviour of the vegetation**

Best et al. (2011)  
*Geosci. Model Dev.*  
Clark et al. (2011)  
*Geosci. Model Dev.*

- 
- ability of plants (within any one PFT) to acclimate or adapt to environmental changes
  - stomatal limitation of photosynthesis **only driven by environmental variables**

Prentice et al. (2014)  
Wang et al. (2017)  
Stocker et al. (in revision)





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Two different model configurations for stomatal limitation of photosynthesis



vn4.6

**Jacobs (1994): JAC**

$$g_s = 1.6RT_{leaf} \frac{A \beta}{c_a - c_i}$$

$$c_i = (c_a - \Gamma^*) \frac{c_i}{c_a} \left( 1 - \frac{D}{D_{crit}} \right) + \Gamma^*$$

$\beta$ : soil moisture stress factor (unitless)

$R$ : universal gas constant ( $\text{J K}^{-1} \text{mol}^{-1}$ )

$T_{leaf}$ : leaf surface temperature ( $^{\circ}\text{K}$ )

$\Gamma^*$ :  $\text{CO}_2$  photorespiration compensation point (Pa)

$A$ : potential leaf net assimilation rate ( $\mu\text{mol mol}^{-1}$ )

Oliver et al. (2018) *Biogeosci.*

Best et al. (2011) *Geosci. Model Dev.*

Clark et al. (2011) *Geosci. Model Dev.*

**Medlyn et al. (2011): MED**

$$g_s \approx g_0 + \left( 1 + \frac{g_1}{\sqrt{D}} \right) \frac{A}{c_a}$$

$$c_i = c_a \left( \frac{g_1}{g_1 + \sqrt{D}} \right)$$

$D$ : leaf-to-air vapour pressure deficit (Pa)

$D_{crit}$ : critical leaf-to-air vapour pressure deficit (Pa)

$g_1$ : sensitivity of  $g_s$  to assimilation rate

+ Farquhar-Collatz photosynthesis model

+ canopy  $A$  ( $\approx$  GPP) estimated with big leaf approach  
(scaled by LAI using Beer's law)

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**Least-cost hypothesis (LC):**

$$c_i = c_a \left( \frac{\xi}{\xi + \sqrt{D}} \right)$$

$$\xi = \sqrt{b} \frac{K}{1.6\eta^*}$$

$D$ : leaf-to-air vapour pressure deficit (Pa)  
 $b$ : ratio of dimensionless cost factors for  
 carboxylation and transpiration  
 $\eta^*$ : viscosity of water relative to its value  
 at 25°C  
 $K$ : effective Michaelis-Menten coefficient  
 for Rubisco-limited photosynthesis (Pa)

Prentice et al. (2014)

Wang et al. (2017)

Stocker et al. (in revision)

**Coordination hypothesis:**

$$GPP = I_{abs} \cdot \phi_0 \cdot m \sqrt{[1 - (c^*/m)^{2/3}]}$$

$$m = \frac{(c_a - \Gamma^*)}{\left\{ c_a + 2\Gamma^* + 3\Gamma^* \sqrt{[1.6 \cdot \eta^* \cdot D \cdot b^{-1} (K + \Gamma^*)^{-1}]} \right\}}$$

$\phi_0$  is the intrinsic quantum yield (g C / mol)

$I_{abs}$  is the absorbed photosynthetic photon flux density  
 (PPFD\*fAPAR, mol /m<sup>2</sup>/s)

fAPAR: fraction of absorbed photosynthetically active  
 radiation (unitless)

$\Gamma^*$  is the photorespiratory compensation point (Pa)

$c^* \approx 0.41$  is estimated from observed  $J_{max}:Vc_{max}$  ratios  
 proportional to the unit carbon cost for the maintenance of  
 electron transport capacity

But no explicit  
 prediction of  
 transpiration yet!

**P model**

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- WATCH-WFDEI data (Weedon et al. 2014) as input + atmospheric CO<sub>2</sub> from Scripps
  - 1. **leaf level:** at > 100 TR sites with carbon isotope data ( $\delta^{13}\text{C}_{\text{TR}}$ ) compilation from Lavergne et al. (in revision)
  - 2. **ecosystem level:** at 34 EC flux sites with > 6 years of records representing forest ecosystems (FLUXNET dataset)
- Model-data comparisons over common 1991-2014 period:  $c_a$  increase by 43 ppm

Model	Parameter	Broadleaf	Needleleaf	References
Jacobs (JAC)	$D_{\text{crit}}$ (kg kg <sup>-1</sup> )	0.09	0.06	Oliver et al. (2018)
Medlyn (MED)	$g_1$ (kPa <sup>0.5</sup> )	3.22	2.22	Oliver et al. (2018)
Prentice (LC)	$b$ (unitless)	146		Smith et al. (2019)

## Coupling the Carbon & Water Cycles

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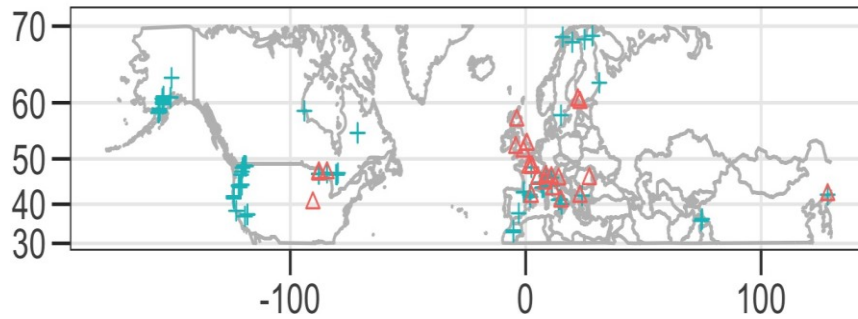
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### Leaf level

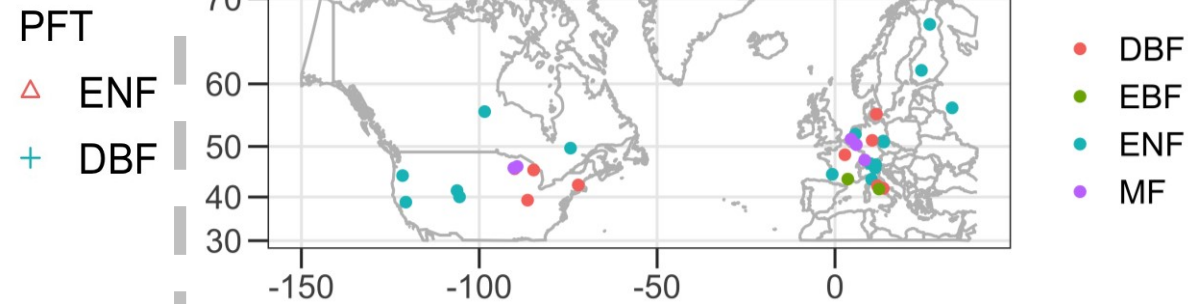


$$\frac{c_i}{c_a} = \frac{\left( \frac{\delta^{13}CO_2 - (\delta^{13}C_{TR} - d)}{1 + (\delta^{13}C_{TR} - d)/1000} \right) - a + f \frac{\Gamma^*}{c_a}}{b - a}$$

$$WUE = \frac{c_a}{1.6 \cdot D} \cdot \left( 1 - \frac{c_i}{c_a} \right)$$

- $\delta^{13}CO_2$ : stable carbon isotopic composition of atmospheric  $CO_2$  (‰)
- $\Gamma^*$ :  $CO_2$  photorespiration compensation point (Pa)
- $a$ : fractionation due to  $CO_2$  diffusion in air = 4.4 ‰
- $b$ : fractionation due to effective Rubisco carboxylation = 30‰
- $f$ : fractionation due to photorespiration = 8‰
- $d$ : post-photosynthetic fractionations = 2.1‰

### Ecosystem level



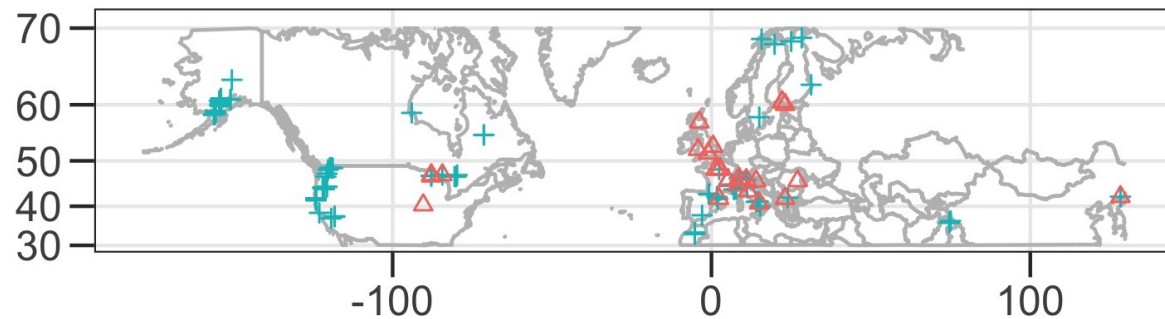
$$eWUE = \frac{GPP}{ET} = \frac{GPP}{LE} \lambda_v$$

$\lambda_v$ : latent heat of vaporization ( $kJ\ kg^{-1}$ )  
 LE: latent heat flux ( $W\ m^{-2}$ )

- Filtering and processing with R package bigleaf (Knauer et al. 2018 PlosOne)
- Aggregation over summer months (June-August)

## Leaf level

1991-2014

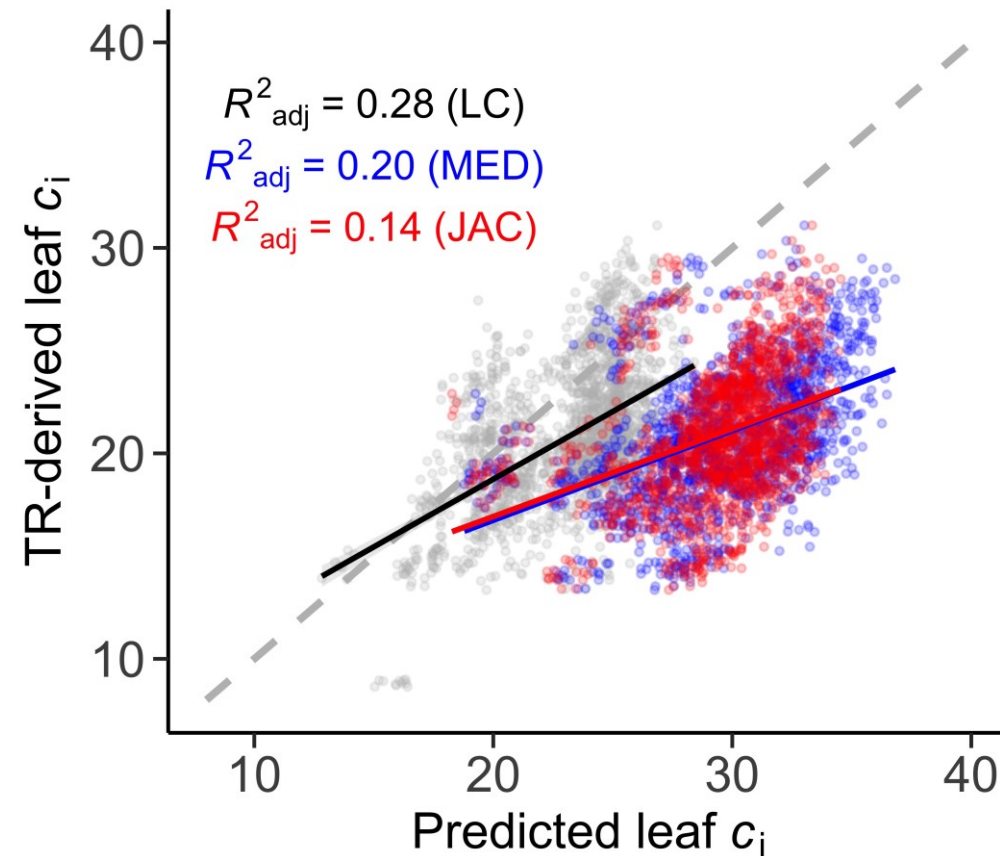


PFT

△ ENF

+ DBF

$$\begin{aligned} \text{(JAC)} \quad c_i &= (c_a - \Gamma^*) \frac{c_i}{g_1^{c_a}} \left( 1 - \frac{D}{D_{crit}} \right) + \Gamma^* \\ \text{(MED)} \quad c_i &= c_a \left( \frac{g_1^{c_a}}{g_1 + \sqrt{D}} \right) \\ \text{(LC)} \quad c_i &= c_a \left( \frac{\xi}{\xi + \sqrt{D}} \right) \end{aligned}$$



## Coupling the Carbon & Water Cycles

Vegetation models & Observations

Observations

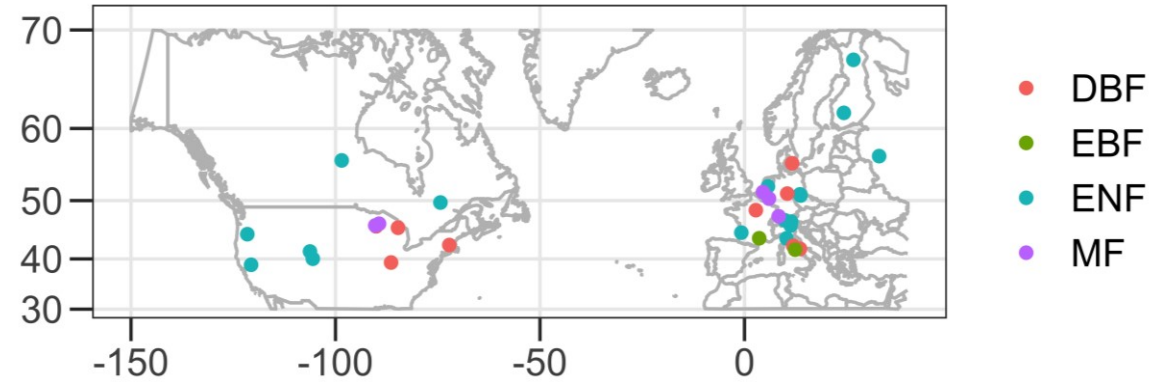
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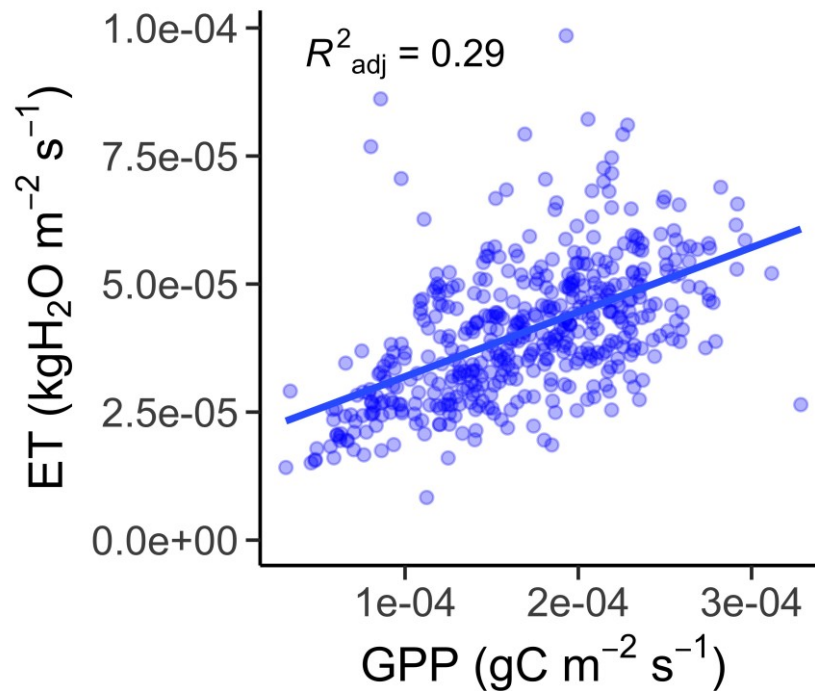
Next steps

### Ecosystem level

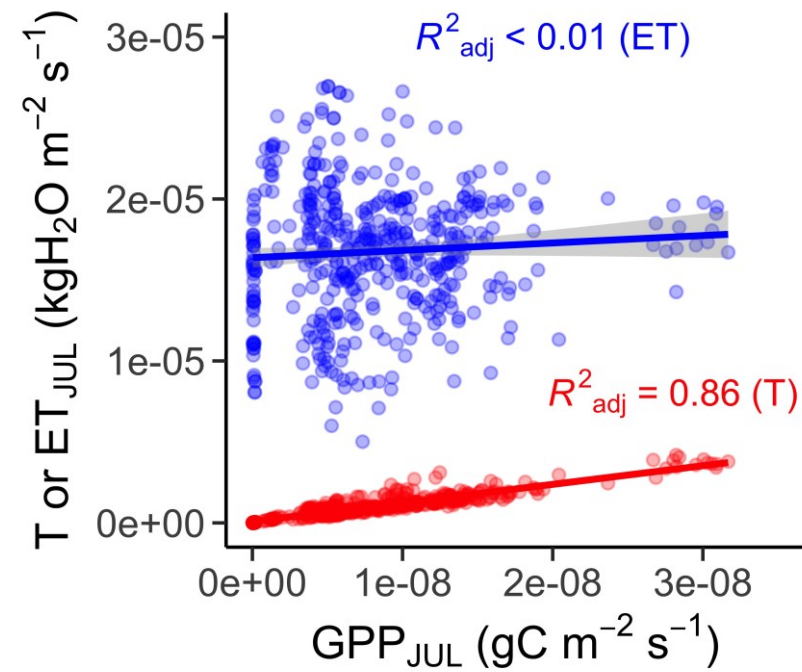
1991-2014



### EC fluxes



### Predictions



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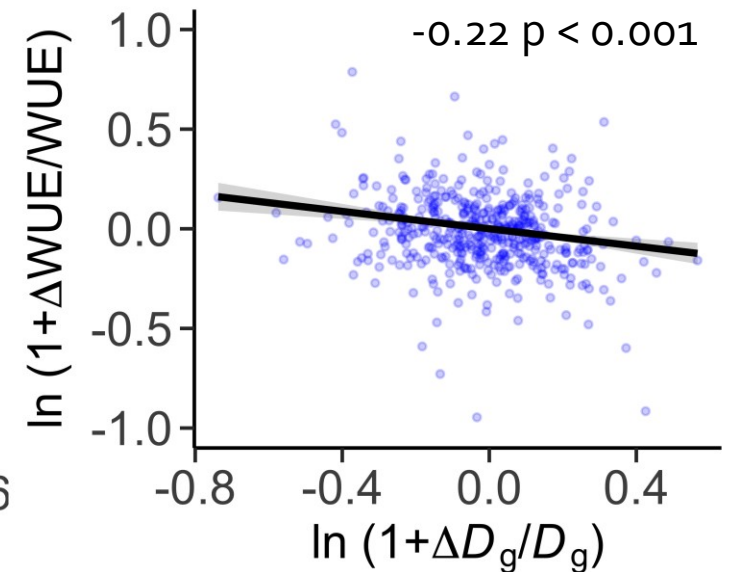
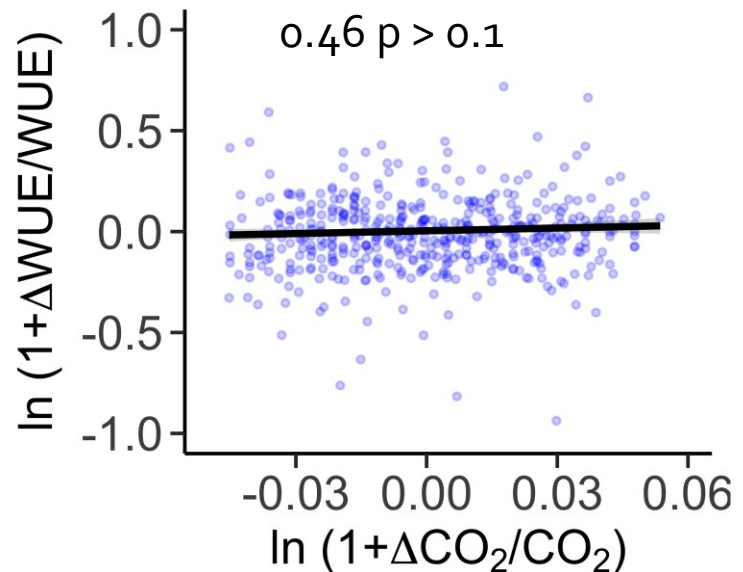
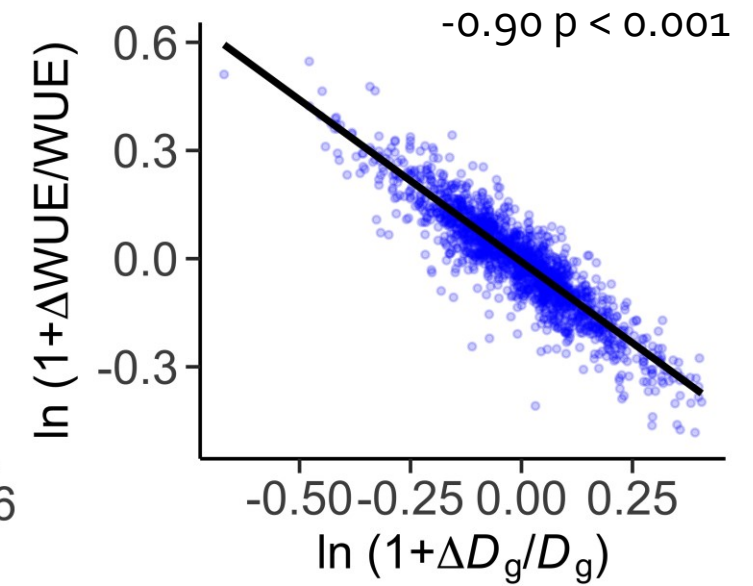
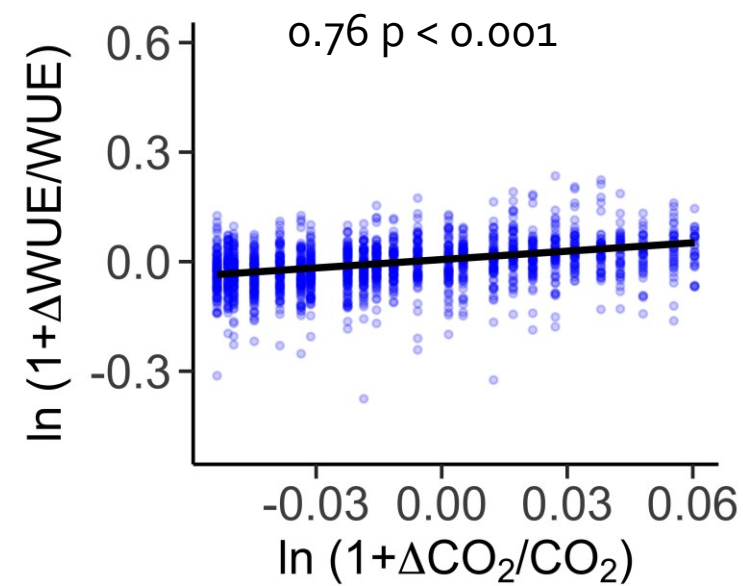
Partial residuals over 1991-2014

## Leaf-level

$$WUE = \frac{c_a}{1.6 \cdot D} \cdot \left(1 - \frac{c_i}{c_a}\right)$$

## Ecosystem-scale

$$eWUE = \frac{GPP}{ET} = \frac{GPP}{LE} \lambda_v$$



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Spatial scale	Type	Driver	Estimate	SE	<i>p</i> value	% of $R^2$ (unique)	% of $R^2$ (unique + common)	$R^2$
Leaf level	OBS-TR	CO <sub>2</sub>	<b>0.76</b>	0.041	<0.001	3.2	0.1	<b>0.82</b>
		<i>D</i>	<b>-0.90</b>	0.010	<0.001	47.1	96.8	
	SIMU LC	CO <sub>2</sub>	<b>1.04</b>	0.025	<0.001	6.3	0.9	<b>0.91</b>
		<i>D</i>	<b>-0.84</b>	0.006	<0.001	31.6	91.2	
	SIMU MED	CO <sub>2</sub>	<b>1.17</b>	0.112	<0.001	4.4	0.5	<b>0.38</b>
		<i>D</i>	<b>-0.91</b>	0.027	<0.001	57.1	68.8	
	SIMU JAC	CO <sub>2</sub>	<b>1.36</b>	0.110	<0.001	7.1	1.7	<b>0.39</b>
		<i>D</i>	<b>-0.90</b>	0.027	<0.001	56.2	91.9	



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		<i>D</i>	<b>-0.22</b>	0.048	<0.001	99.0	92.1	
Using ET flux	SIMU MED	CO <sub>2</sub>	<b>0.29</b>	0.472	0.533	5.3	6.9	<b>&lt;0.01</b>
		<i>D</i>	<b>0.22</b>	0.083	0.009	93.3	95.1	
	SIMU JAC	CO <sub>2</sub>	<b>0.27</b>	0.469	0.561	4.8	6.5	<b>&lt;0.01</b>
		<i>D</i>	<b>0.21</b>	0.082	0.011	93.8	94.9	

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		<i>D</i>	<b>-0.10</b>	0.037	0.009	9.7	8.0	
	SIMU JAC	CO <sub>2</sub>	<b>1.83</b>	0.251	<0.001	91.3	89.6	<b>0.10</b>
		<i>D</i>	<b>-0.11</b>	0.044	0.014	10.4	8.6	

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**Leaf level:** all models of stomatal limitation of photosynthesis (i.e. LC, JAC or MED) reproduce reasonably well the relative contributions from  $c_a$  and  $D$  to changes in leaf WUE



**Ecosystem level:** JULES tends to assign erroneously a positive influence of  $D$  to changes in eWUE when using LE flux, or overestimate the influence of  $CO_2$  when using the transpiration flux



Need to refine processes modelled at the ecosystem level → testing new formulations for GPP and ET against EC flux measurements



Implementation of transpiration in the P model done by colleagues will allow predictions of eWUE

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RUNNING LONGER  
SIMULATIONS WITH JULES  
TO ASSESS LONG-TERM  
PREDICTIVE SKILLS



TESTING IMPLEMENTATION OF  
LC HYPOTHESIS IN JULES AND  
COMPARING SIMULATIONS WITH  
CARBON ISOTOPE DATA



IMPLEMENTATION OF CARBON  
ISOTOPES IN JULES



IMPROVING  
PREDICTIONS OF T AND  
GPP IN JULES?

# Acknowledgements

## Coupling the Carbon & Water Cycles



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FLUXNET contributors



All colleagues providing carbon isotopes data from tree rings

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# P Model: a Simple Optimality model

## Input data

Atmospheric CO<sub>2</sub>,  
temperature, vapour  
pressure deficit

Incoming shortwave  
radiation, fAPAR

Elevation

## P model

### Least-cost (LC) hypothesis

leaves minimize the  
summed unit costs of  
transpiration and  
carboxylation

### Coordination hypothesis

photosynthesis equally  
limited by electron  
transport and  
carboxylation under  
average environmental  
conditions

## Outputs

$\chi$   
Leaf-internal to  
ambient CO<sub>2</sub>  
concentrations

**GPP**  
Gross primary  
production

### *Spatial Resolution*

#### Site

(e.g. FLUXNET, tree-ring sites)

#### Region

(e.g. high resolution satellite data)

#### Global

(e.g. MERIS, MODIS, ECMWF)

### *Temporal Resolution*

Half-hourly to daily

Monthly

Annual